

# Prospects of experimentally reachable beyond Standard Model physics in inverse seesaw motivated non-SUSY SO(10) GUT

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UNICOS - 2014

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May 15, 2014

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<sup>1</sup>Parida, arXiv:1112.1826, arXiv:1302.0672(S. Patra), arXiv:1401.1412(P. K. Sahu) 

- Introduction
- Grand unification,  $SO(10)$  etc
- Non-SUSY  $SO(10)$  with TeV scale inverse seesaw
- Extended non-SUSY  $SO(10)$  with extended inverse seesaw
- Summary

# Introduction

## Standard Model particle content

| Spin=1      |                               |                                                            |                                                            |                                                            |
|-------------|-------------------------------|------------------------------------------------------------|------------------------------------------------------------|------------------------------------------------------------|
| Gluons      | $G_{\mu}^a, a = 1, 2 \dots 8$ | (1,0,8)                                                    | $SU(3)_C$                                                  | $g_s$                                                      |
| Weak Bosons | $W_{\mu}^i, i = 1, 2, 3$      | (3,0,1)                                                    | $SU(2)_L$                                                  | $g$                                                        |
| Hyperon     | $B_{\mu}$                     | (1,0,1)                                                    | $U(1)_Y$                                                   | $g'$                                                       |
| Spin=1/2    |                               |                                                            |                                                            |                                                            |
| Quarks      | (2, 1/6, 3)                   | $\begin{pmatrix} u^{\kappa} \\ d^{\kappa} \end{pmatrix}_L$ | $\begin{pmatrix} c^{\kappa} \\ s^{\kappa} \end{pmatrix}_L$ | $\begin{pmatrix} t^{\kappa} \\ b^{\kappa} \end{pmatrix}_L$ |
|             | (1, 2/3, 3)                   | $u_R^{\kappa}$                                             | $c_R^{\kappa}$                                             | $t_R^{\kappa}$                                             |
|             | (1, -1/3, 3)                  | $d_R^{\kappa}$                                             | $s_R^{\kappa}$                                             | $b_R^{\kappa}$                                             |
| Leptons     | (2, -1/2, 1)                  | $\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$               | $\begin{pmatrix} \nu_{\mu} \\ \mu \end{pmatrix}_L$         | $\begin{pmatrix} \nu_{\tau} \\ \tau \end{pmatrix}_L$       |
|             | (1, -1, 1)                    | $e_R$                                                      | $\mu_R$                                                    | $\tau_R$                                                   |
| Spin=0      |                               |                                                            |                                                            |                                                            |
| Higgs       | (2, -1/2, 1)                  | $\begin{pmatrix} H^0 \\ H^- \end{pmatrix}$                 |                                                            |                                                            |

Table : The Standard Model particles.

# Introduction

## Standard Model (Excellencies)

$$SU(2)_L \otimes U(1)_Y \otimes SU(3)_C$$

- Tested at  
LEP ( $e^+e^-$ ), SLC ( $e^+e^-$ ), Tevatron ( $p\bar{p}$ ), HERA ( $e^-p$ ), PEP-II ( $e^+e^-$ ), KEKB ( $e^+e^-$ ) and recently at LHC ( $pp$ ).
- 20 GeV to 8 TeV Explored.
- All the particles predicted by the Standard Model, namely  
 $\tau$  (1975),  $\nu_\tau$  (2000),  $c$  (1974),  $b$  (1977),  $t$  (1995), gluons (1979),  $W$ ,  $Z$  (1983) and Higgs (2012),  
have been discovered.
- Fits precisely.

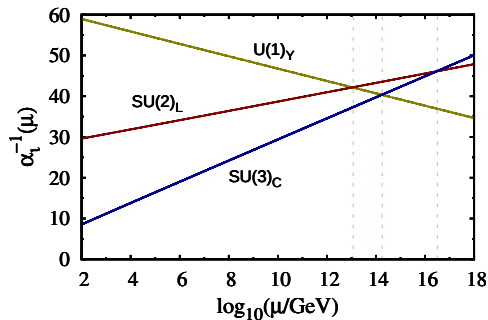
# Introduction

## Standard Model (Deficiencies)

- Neutrino masses and mixings  
(S. Goswami, A. Raychaudhuri, Y. Y. Keum, R. Srivastava)
- Dark Matter (G. Rajasekaran, S. Vempati)
- Baryonic asymmetry of universe
- Flavor problem
- Hierarchy or naturalness problem (R. K. Kaul)
- Gauge symmetry problem
- Charge quantization (B. Bajc, Z. Tavartkiladze)

# Grand unification

Gauge structure of three forces + Higgs Mechanism + A hint from gauge couplings evolution



Gauge coupling evolution

$$\mu \frac{\partial \alpha_i}{\partial \mu} = \frac{b_i}{2\pi} \alpha_i^2 + \mathcal{O}(2) + Yuk. \quad (1)$$

For

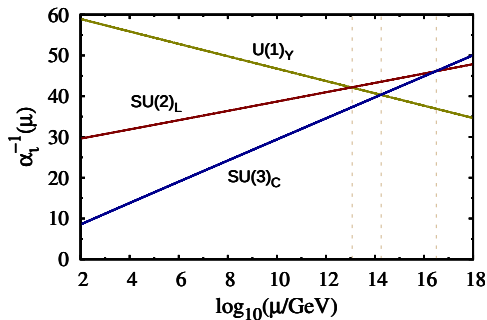
$$SU(2)_L \otimes U(1)_Y \otimes SU(3)_C$$

$$b = (-19/6, 41/10, -7) \quad (2)$$

Borut Bajc

# Grand unification

Gauge structure of three forces + Higgs Mechanism + A hint from gauge couplings evolution



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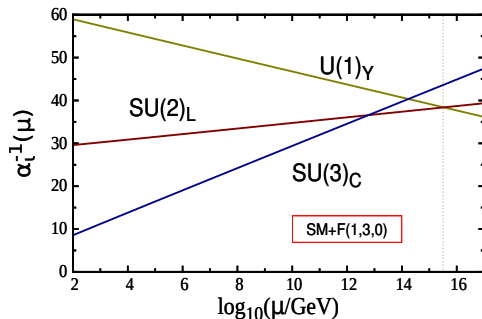
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$$b = (-19/6, 41/10, -7) \quad (2)$$

Borut Bajc

# Grand unification

Simple tuning of unification scale



$F(3, 0, 1)$  at  $M_Z$ .

Gauge coupling evolution

$$\mu \frac{\partial \alpha_i}{\partial \mu} = \frac{b_i}{2\pi} \alpha_i^2 + \mathcal{O}(2) + \text{Yuk.} \quad (3)$$

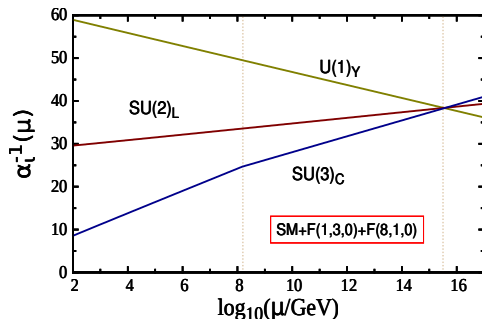
For

$$SU(2)_L \otimes U(1)_Y \otimes SU(3)_C$$

$$b = (-11/6, 41/10, -7) \quad (4)$$

# Grand unification

Simple tuning of unification scale



Borut Bajc, G. Senjanovic, 2007

Gauge coupling evolution

$$\mu \frac{\partial \alpha_i}{\partial \mu} = \frac{b_i}{2\pi} \alpha_i^2 + \mathcal{O}(2) + \text{Yuk.} \quad (5)$$

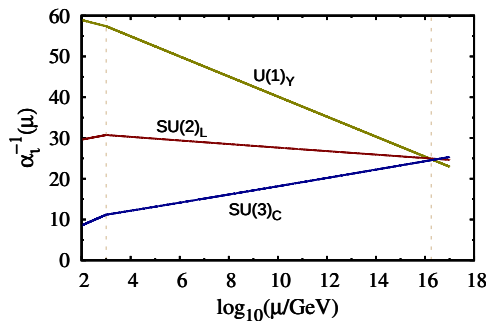
For

$$SU(2)_L \otimes U(1)_Y \otimes SU(3)_C$$

$$b = (-11/6, 41/10, -5) \quad (6)$$

# Grand unification

## Minimal Supersymmetric Standard Model



Below TeV

$$SU(2)_L \otimes U(1)_Y \otimes SU(3)_C$$

$$b = (-19/6, 41/10, -7) \quad (7)$$

Above TeV

$$b = (1, 33/5, -3) \quad (8)$$

Borut Bajc

# Grand unification

## Minimal Supersymmetric Standard Model

- TeV scale SUSY.
- Stabilizes the fine tunings.
- Cold dark matter candidate.<sup>2</sup>
- MSSM+Seesaw extension  $\Rightarrow$  Neutrino parameters || SUSY-GUT.<sup>3</sup>
- But, no SUSY has been seen yet.<sup>4</sup>

C.S. Aulakh, S. Vempati, U. A. Yajnik, K. S. Babu, R. Mohapatra. . .

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<sup>2</sup>Fowlie et al, Han et al

<sup>3</sup>Mohapatra, Altarelli, Babu, Senjanovic, Aulakh, Ma

<sup>4</sup>ATLAS and CMS results

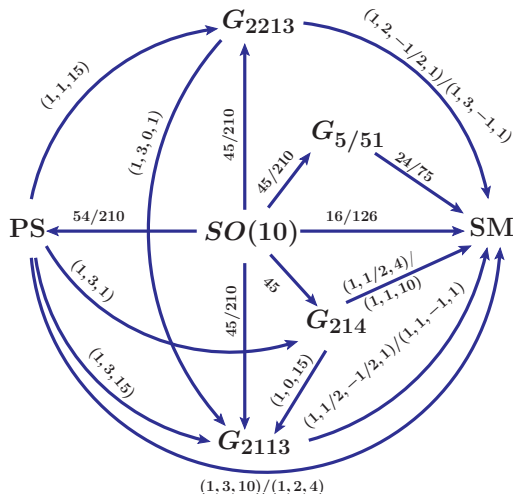
# Grand unification

non-SUSY

- Intermediate symmetries for unification of interactions.
- Low energy predictions?

# Grand unification

From  $SO(10)$  to SM



$$G_{13} = U(1)_{\text{QED}} \otimes SU(3)_C$$

$$G_{5/51} = SU(5)/SU(5) \otimes U(1)_X$$

$$G_{213} = SU(2)_L \otimes U(1)_Y \otimes SU(3)_C \quad (\text{SM})$$

$$G_{214} = SU(2)_L \otimes U(1)_X \otimes SU(4)_C$$

$$G_{224} = SU(2)_L \otimes SU(2)_R \otimes SU(4)_C \quad (\text{PS})$$

$$G_{224D} = SU(2)_L \otimes SU(2)_R \otimes SU(4)_C \otimes D \quad (\text{PSD})$$

$$G_{2113} = SU(2)_L \otimes U(1)_{B-L} \otimes U(1)_R \otimes SU(3)_C$$

$$G_{2213} = SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L} \otimes SU(3)_C \quad (\text{LR})$$

$$G_{2213D} = SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L} \otimes SU(3)_C \otimes D \quad (\text{LRD})$$

# Grand unification

## Nomenclature

$$(1, 1, 15)_{G_{224}} \subset 45, 210$$

$$(1, 3, 0, 1)_{G_{2213}} \subset (1, 3, 1)_{G_{224}} \subset 45$$

$$(1, 0, 15)_{G_{214}} \subset (1, 3, 15)_{G_{224}} \subset 210$$

$$(1, 3, 0, 1)_{G_{2213}} \subset (1, 3, 15)_{G_{224}} \subset 210$$

$$(1, 1, -1, 1)_{G_{2113}} \subset (1, 1, 10)_{G_{214}} \subset (1, 3, 10)_{G_{224}} \subset 126^{\dagger}$$

$$(1, 1, -1, 1)_{G_{2113}} \subset (1, 3, -1, 1)_{G_{2213}} \subset (1, 3, 10)_{G_{224}} \subset 126^{\dagger}$$

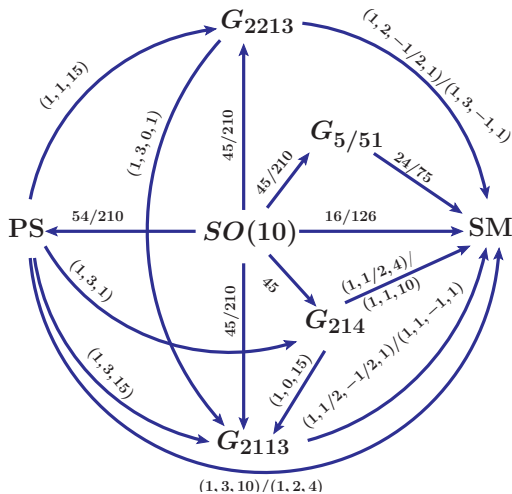
$$(1, 1/2, -1/2, 1)_{G_{2113}} \subset (1, 1/2, 4)_{G_{214}} \subset (1, 2, 4)_{G_{224}} \subset 16^{\dagger}$$

$$(1, 1/2, -1/2, 1)_{G_{2113}} \subset (1, 2, -1/2, 1)_{G_{2213}} \subset (1, 2, 4)_{G_{224}} \subset 16^{\dagger}$$

**Table :** The multiplets participating in SSB by acquiring VEVs in the invariant direction of the residual symmetry.

# Grand unification

From  $SO(10)$  to SM



# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

The Model<sup>6</sup>

Required multiplets

$$(3 \otimes 16 + 3 \otimes 1)_F + (2 \otimes 10 + 16 + 45)_H + 45_G \quad (10)$$

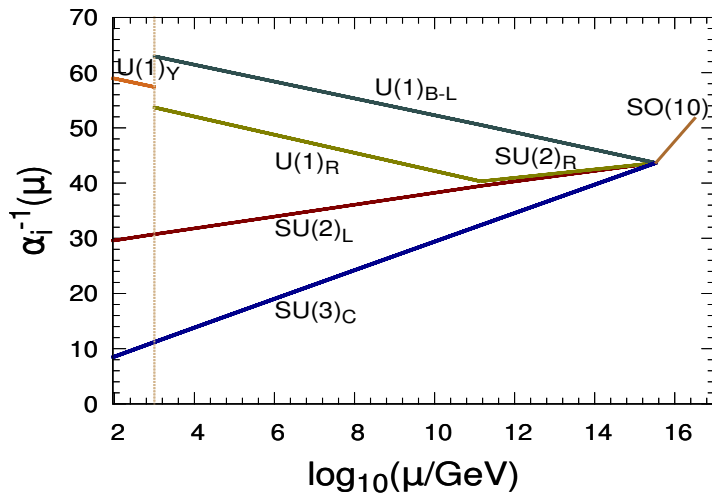
- Two step breaking scheme

$$\textcolor{brown}{SO}(10) \xrightarrow[45]{M_U} G_{2213} \xrightarrow[45]{M_R^+} \textcolor{violet}{G}_{2113} \xrightarrow[16]{M_R^0} \text{SM} \quad (11)$$

<sup>6</sup>SUSY analog: Bhupal dev, Mohapatra, 2010

# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

Excellent Gauge coupling unification



●  $M_{Z'} = 1\text{TeV}$ ,  $M_U = 10^{15.53}\text{ GeV}$ ,  $M_R^+ = 10^{11.15}\text{ GeV}$

# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

Proton lifetime, Experimentally verifiable unification scale

- $\Gamma(p \rightarrow e^+ \pi^0) \propto \left( \frac{g_G^4}{M_U^4} \right)$

- **Exp bound:**  $1.01(1.4) \times 10^{34} \text{ yrs},$  <sup>7</sup>

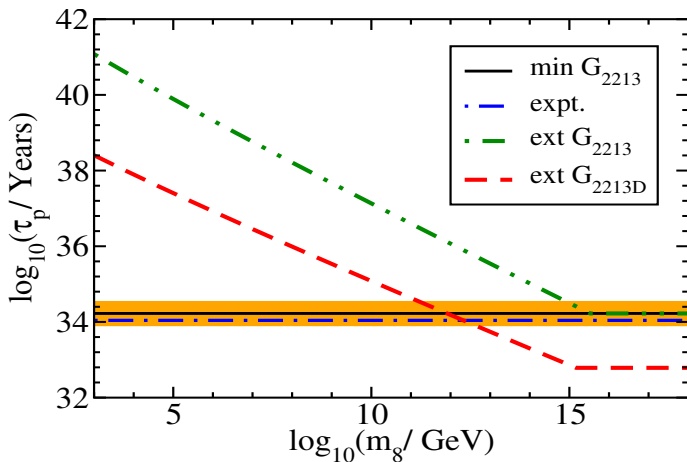
- **Model Prediction:**  $2 \times 10^{34 \pm 0.32} \text{ yrs}$

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<sup>7</sup>Nishino et al (2009), Babu in arXiv:1205.2671

# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

Saving the model



- Enhancement in proton lifetime is due to presence of a color octet scalar  $(1,0,8)$  in the model extension.

# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

Yukawa Lagrangian, seesaw matrix

$$\begin{aligned}\mathcal{L}_{Yuk} &= Y^a 16.16.10_H^a + y_\chi 16.1.16_H^\dagger + \mu_S 1.1 \\ &\supset Y^a \bar{\psi}_L \psi_R \Phi^a + y_\chi \bar{\psi}_R S \chi_R + \mu_S S^T S + h.c. \quad (12)\end{aligned}$$

- In  $(\nu, N^C, S)^T$  basis the full neutrino mass matrix<sup>8</sup> is

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & M_D & 0 \\ M_D^T & 0 & M \\ 0 & M^T & \mu_S \end{pmatrix}_{9 \times 9} \quad (13)$$

- $M_D = Y_\nu v_u$ ,  $M = Y_\chi v_\chi$  and  $\mu_S$  are unknown at low energy.
- $\mu_S \ll M_D < M$ .

S. Vempati, K. S. Babu

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<sup>8</sup>Mohapatra (1986,2010)

# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

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S. Vempati, K. S. Babu

<sup>8</sup>Mohapatra (1986,2010)

<sup>9</sup>Grimus(2000)

- This complex symmetric matrix can be block diagonalized by a  $9 \times 9$  unitary matrix  $\mathcal{V}$  such that

$$\mathcal{V}^\dagger \mathcal{M}_\nu \mathcal{V}^* = \hat{\mathcal{M}}_\nu = \begin{pmatrix} m_\nu & 0 \\ 0 & M_H \end{pmatrix} \quad (14)$$

where  $m_\nu$  is light neutrino mass matrix and is further diagonalized by a unitary matrix, say, PMNS; and  $M_H$  is the heavy neutrino mass matrix.

# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

## Inverse seesaw

- In  $\mu_S \ll M_D \ll M$  limits, The full diagonalizing matrix looks like

$$\mathcal{V} \simeq \begin{pmatrix} 1 - \frac{1}{2}XX^\dagger & -y & X \\ y^\dagger & 1 - \frac{1}{2}y^\dagger y & \frac{1}{2}y^\dagger X \\ -X^\dagger & \frac{1}{2}X^\dagger y & 1 - \frac{1}{2}X^\dagger X \end{pmatrix} \begin{pmatrix} U_\nu & 0 \\ 0 & U_H \end{pmatrix} \quad (15)$$

where  $y = -\frac{M_D}{M} \frac{\mu_S}{M^T}$  and  $X = \frac{M_D}{M}$ .

- The light and heavy neutrino mass matrices get the form

$$m_\nu \simeq \frac{M_D}{M} \mu_S \left( \frac{M_D}{M} \right)^T \equiv X \mu_S X^T \quad (16)$$

$$M_h \simeq \begin{pmatrix} -M & 0 \\ 0 & M \end{pmatrix} + \mathcal{O}(\mp M_D^2/M) \quad (17)$$

- $|\eta|_{33} \equiv |XX^\dagger|_{33} < [2.7 \times 10^{-3}]^{10}$

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<sup>10</sup>Kanaya, Antusch, Smirnov, Altarelli, Malinsky, Aguila, Schaff etc.

# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

## Inverse seesaw

- In  $\mu_S \ll M_D \ll M$  limits, The full diagonalizing matrix looks like

$$\mathcal{V} \simeq \begin{pmatrix} 1 - \frac{1}{2}XX^\dagger & -y & X \\ y^\dagger & 1 - \frac{1}{2}y^\dagger y & \frac{1}{2}y^\dagger X \\ -X^\dagger & \frac{1}{2}X^\dagger y & 1 - \frac{1}{2}X^\dagger X \end{pmatrix} \begin{pmatrix} U_\nu & 0 \\ 0 & U_H \end{pmatrix} \quad (15)$$

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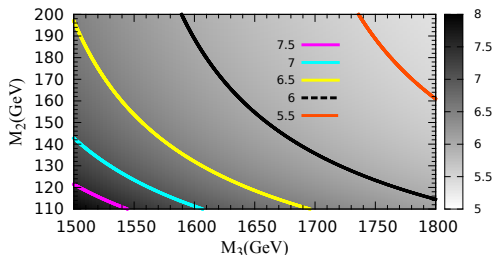
# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

Dirac mass matrix estimation, Non-unitarity constraints on  $M$

$$M_D = \begin{pmatrix} 0.0151 & 0.0674 - 0.0113i & 0.1030 - 0.2718i \\ 0.0674 + 0.0113i & 0.4758 & 3.4410 + 0.0002i \\ 0.1030 + 0.2718i & 3.4410 - 0.0002i & 83.45 \end{pmatrix} \text{ GeV.} \quad (18)$$

Non-unitarity constraint

$$\frac{1}{2} \left[ \frac{0.0845}{M_1^2} + \frac{11.8405}{M_2^2} + \frac{6963.9}{M_3^2} \right] \text{ GeV}^2 < 2.7 \times 10^{-3}, \quad (19)$$



- Heavy neutrino contribute to Lepton flavour violating (LFV) decays<sup>11</sup>

$$\mathcal{L}_{CC} = -\frac{g_{2L}}{\sqrt{2}} \bar{l}_L \gamma^\mu (\mathcal{N} \hat{\nu}^T + \mathcal{K} P^T) W_\mu^- + h.c. \quad (20)$$

$$BR(l_\alpha \rightarrow l_\beta \gamma) \propto \left| \sum_{i=1}^6 \mathcal{K}_{\alpha i} \mathcal{K}_{\beta i}^* \left( \frac{M_i^2}{M_w^2} \right) \right|^2 \quad (21)$$

where  $\mathcal{K} \equiv \mathcal{V}_{3 \times 6} \simeq (0, M_D M^{-1}) U_{6 \times 6}$ .

- LFV decay are severally suppressed in Type-I seesaw scenario.
- The matrix  $(\mathcal{K} \mathcal{K}^\dagger)$  may lead to large LFV decay in inverse seesaw.

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<sup>11</sup>Ilakovac and Pilaftsis (1995)

# Non-SUSY SO(10) with TeV scale $Z'$ and Inverse seesaw

## Estimates of Lepton Flavor Violation

$$\begin{aligned}BR(\mu \rightarrow e\gamma) &= 2.0 \times 10^{-16} (< 5.7 \times 10^{-13}), \\BR(\tau \rightarrow e\gamma) &= 2.2 \times 10^{-14} (< 3.3 \times 10^{-8}), \\BR(\tau \rightarrow \mu\gamma) &= 3.0 \times 10^{-12} (< 4.4 \times 10^{-8}).\end{aligned}\tag{22}$$

Current experimental constraints<sup>12</sup> are given in the brackets.

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<sup>12</sup>MEG (arxiv:1303.0754), Bell (2010, 2011, 2012), BaBar (2009, 2010), PDG (2012)

# Non-SUSY SO(10) with extended Inverse seesaw

## Predictions

- TeV scale  $W_R$ ,  $Z_R$
- $n - \bar{n}$
- Rare Kaon decay
- Lepton flavor violation
- New contribution to  $0\nu\beta\beta$ .

# Non-SUSY SO(10) with extended inverse seesaw

Breaking scheme<sup>13</sup>

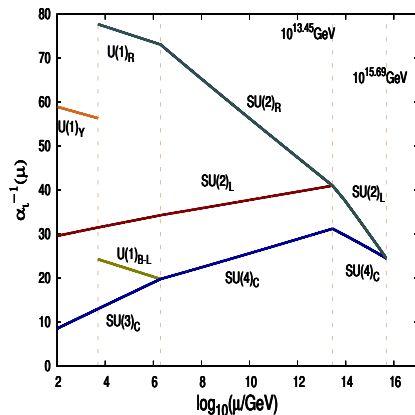
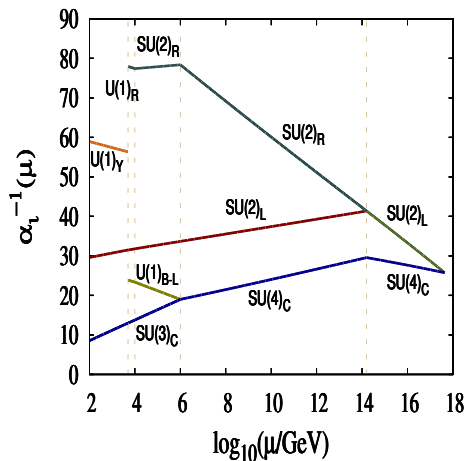
$$\begin{array}{ll}
 SO(10) & \xrightarrow[54]{M_U} G_{224D} \parallel g_{2L} = g_{2R} \\
 & \xrightarrow[210]{M_P} G_{224} \parallel g_{2L} \neq g_{2R} \\
 & \xrightarrow[45]{M_C} G_{2213} \\
 & \xrightarrow[210]{M_R^+} G_{2113} \\
 & \xrightarrow[126+16]{M_R^0} SM \\
 & \xrightarrow[10]{M_Z} G_{13}.
 \end{array} \quad (23)$$

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 SO(10) & \xrightarrow[54]{M_U} G_{224D} \parallel g_{2L} = g_{2R} \\
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 & \xrightarrow[210]{M^C} G_{2113} \\
 & \xrightarrow[126+16]{M_R^0} SM \\
 & \xrightarrow[10]{M_Z} G_{13}.
 \end{array} \quad (24)$$

<sup>13</sup>Chang et al (1985), Chang and Kumar (1986)

# Non-SUSY SO(10) with extended inverse seesaw

Gauge coupling unification



# Non-SUSY SO(10) with extended inverse seesaw

Proton decay prediction in the model at left

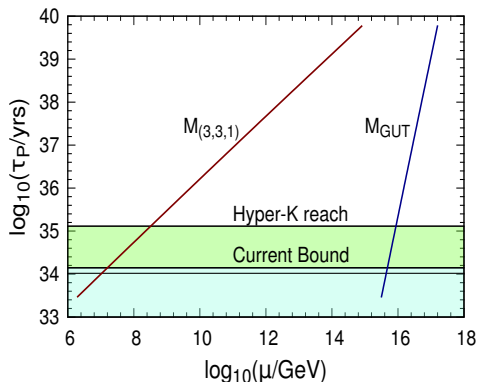


Figure : Dependence of unification scale on the mass of bi-triplet  $(3,3,1)$  in the model at left.

# Non-SUSY SO(10) with extended inverse seesaw

## Extended inverse seesaw

$$\begin{aligned}\mathcal{L}_{\text{Yuk}} &= Y^\ell \bar{\psi}_L \psi_R \Phi + f \psi_R^c \psi_R \Delta_R + F \bar{\psi}_R S \chi_R \\ &+ S^\top \mu_S S + \text{h.c.}\end{aligned}\tag{25}$$

- In the  $(\nu, S, N^c)^T$  basis the mass matrix is

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & 0 & M_D \\ 0 & \mu_S & M \\ M_D^T & M^T & M_N \end{pmatrix}\tag{26}$$

- Here  $M_D = Y^\ell \langle \Phi \rangle$ ,  $M_N = f \langle \Delta_R^0 \rangle$ ,  $M = F \langle \chi_R^0 \rangle$ .

# Non-SUSY SO(10) with extended inverse seesaw

## Extended inverse seesaw

$$\begin{aligned}\mathcal{L}_{\text{Yuk}} &= Y^\ell \bar{\psi}_L \psi_R \Phi + f \psi_R^c \psi_R \Delta_R + F \bar{\psi}_R S \chi_R \\ &+ S^\top \mu_S S + \text{h.c.}\end{aligned}\tag{25}$$

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- Here  $M_D = Y^\ell \langle \Phi \rangle$ ,  $M_N = f \langle \Delta_R^0 \rangle$ ,  $M = F \langle \chi_R^0 \rangle$ .

# Non-SUSY SO(10) with extended inverse seesaw

## Extended inverse seesaw

$$m_\nu \simeq M_D M^{-1} \mu_S (M_D M^{-1})^T \quad (27)$$

$$m_S \simeq \mu_S - M M_N^{-1} M^T \quad (28)$$

$$\& \quad m_N \simeq M_N. \quad (29)$$

# Non-SUSY SO(10) with extended inverse seesaw

## Extended inverse seesaw

The collective mixing matrix is

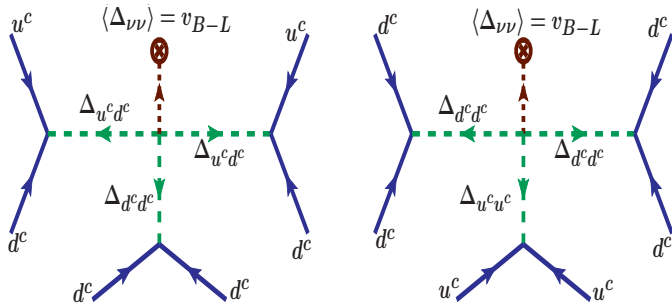
$$\begin{aligned}\mathcal{V} &\equiv \begin{pmatrix} \mathcal{V}_{\alpha i}^{\nu\hat{\nu}} & \mathcal{V}_{\alpha j}^{\nu\hat{S}} & \mathcal{V}_{\alpha k}^{\nu\hat{N}} \\ \mathcal{V}_{\beta i}^{S\hat{\nu}} & \mathcal{V}_{\beta j}^{S\hat{S}} & \mathcal{V}_{\beta k}^{S\hat{N}} \\ \mathcal{V}_{\gamma i}^{N\hat{\nu}} & \mathcal{V}_{\gamma j}^{N\hat{S}} & \mathcal{V}_{\gamma k}^{N\hat{N}} \end{pmatrix} \\ &\simeq \begin{pmatrix} (1 - \frac{1}{2}XX^\dagger) U_\nu & (X - \frac{1}{2}ZY^\dagger) U_S & Z U_N \\ -X^\dagger U_\nu & (1 - \frac{1}{2}\{X^\dagger X + YY^\dagger\}) U_S & (Y - \frac{1}{2}X^\dagger Z) U_N \\ y^* X^\dagger U_\nu & -Y^\dagger U_S & (1 - \frac{1}{2}Y^\dagger Y) U_N \end{pmatrix},\end{aligned}\tag{30}$$

where  $X = M_D M^{-1}$ ,  $Y = M M_N^{-1}$ ,  $Z = M_D M_N^{-1}$ , and  $y = M^{-1} \mu_S$

- ★ Lepton flavor violation predictions are same as discussed in previous model.
- ★ The predicted values are only 3 – 6 order less than present experimental bound.

# Non-SUSY SO(10) with extended inverse seesaw

$n - \bar{n}$  Oscillation



$$\text{Amp}_{n-\bar{n}}^{(a)} = \frac{f_{11}^3 \lambda v_{B-L}}{M_{\Delta_{u^c d^c}}^4 M_{\Delta_{d^c d^c}}^2}, \quad \text{Amp}_{n-\bar{n}}^{(b)} = \frac{f_{11}^3 \lambda v_{B-L}}{M_{\Delta_{d^c d^c}}^4 M_{\Delta_{u^c u^c}}^2},^{14} \quad (31)$$

where  $f_{11} = (f_{\Delta_{u^c d^c}})_{11} = (f_{\Delta_{d^c d^c}})_{11} = (f_{\Delta_{u^c u^c}})_{11} \subset 126_H$

$\sim \mathcal{O}(0.1) - \mathcal{O}(1)$ .

<sup>14</sup>Babu et al (2013)

# Non-SUSY SO(10) with extended inverse seesaw

## $n - \bar{n}$ Oscillation

The  $n - \bar{n}$  mixing mass element

$$\delta m_{n\bar{n}} = \left(10^{-4} \text{ GeV}^6\right) \cdot W_{B=2}. \quad (32)$$

where  $W_{B=2} = \text{Amp}^{(a)} + \text{Amp}^{(b)}$ .

The experimentally measurable mixing time

$$\begin{aligned} \tau_{n-\bar{n}} &= \frac{1}{\delta m_{n\bar{n}}} \\ &= 10^8 - 10^{10} \text{ secs.} \end{aligned} \quad (33)$$

★ Accessible at ongoing experiments.

# Non-SUSY SO(10) with extended inverse seesaw

Rare Kaon decay

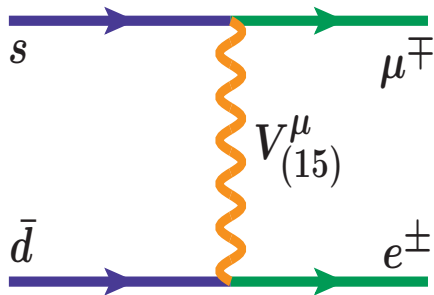


Figure :  $K_L^0 \rightarrow \mu^\mp e^\pm$

# Non-SUSY SO(10) with extended inverse seesaw

## Rare Kaon decay

$$\text{Br}(K_L \rightarrow \mu \bar{e})_{\text{expt.}} \equiv \frac{\Gamma(K_L \rightarrow \mu^\pm e^\mp)}{\Gamma(K_L \rightarrow \text{all})} < 4.7 \times 10^{-12}, \quad (34)$$

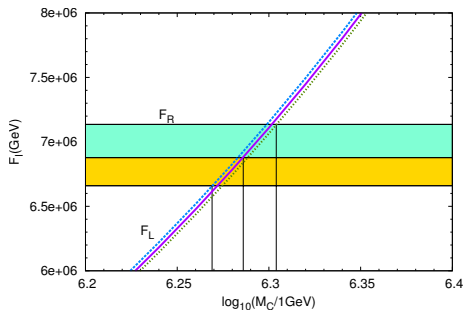
$$\text{Br}(K_L \rightarrow \mu \bar{e}) = \frac{4\pi^2 \alpha_s^2(M_C) m_K^4 R}{G_F^2 \sin^2 \theta_C m_\mu^2 (m_s + m_d)^2 M_C^4} \cdot^{15} \quad (35)$$

$$R = \left[ R_{2113} R_{213}^{(6)} R_{213}^{(5)} R_{QCD}^{(5)} R_{QCD}^{(4)} R_{QCD}^{(3)} \right]^{-2} \quad (36)$$

$$\left[ F_L(M_C, M_R^0) \right]_{\text{Model dependent}} = [F_R]_{\text{Model independent}} \quad (37)$$

# Non-SUSY SO(10) with extended inverse seesaw

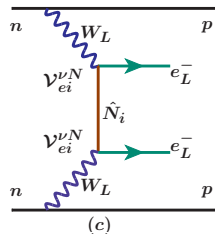
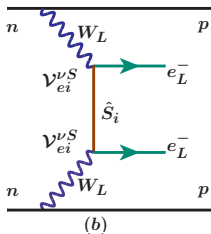
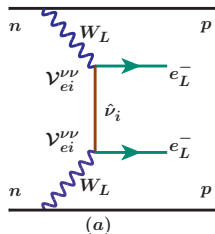
## Rare Kaon decay



$$M_C > 1.86 \times 10^6 \text{ GeV}. \quad (38)$$

# Non-SUSY SO(10) with extended inverse seesaw

$0\nu\beta\beta$ <sup>16</sup>

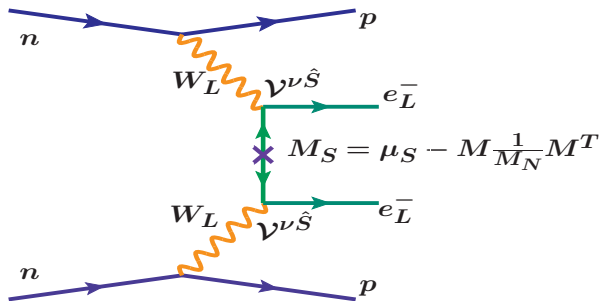


<sup>16</sup>Bilenki, Mohapatra, Mitra, Rodejohan, Senjanovic, Vergados, Vissani etc

# Non-SUSY SO(10) with extended inverse seesaw

Sterile neutrino contribution to  $0\nu\beta\beta$

$$\mathcal{A}_S^{LL} \propto \frac{1}{M_{W_L}^4} \sum_{j=1,2,3} \frac{(\nu_{ej}^{\nu\hat{S}})^2}{m_{S_j}} \quad (39)$$



# Non-SUSY SO(10) with extended inverse seesaw

Sterile neutrino contribution to  $0\nu\beta\beta$

$$\begin{aligned}\mathcal{A}_\nu^{LL} &\propto \frac{1}{M_{W_L}^4} \sum_{i=1,2,3} \frac{(\mathcal{V}_{ei}^{\nu\hat{\nu}})^2 m_{\nu_i}}{p^2}, \\ \mathcal{A}_S^{LL} &\propto \frac{1}{M_{W_L}^4} \sum_{j=1,2,3} \frac{(\mathcal{V}_{ej}^{\nu\hat{S}})^2}{m_{S_j}}, \\ \mathcal{A}_N^{LL} &\propto \frac{1}{M_{W_L}^4} \sum_{k=1,2,3} \frac{(\mathcal{V}_{ek}^{\nu\hat{N}})^2}{m_{N_k}},\end{aligned}\tag{40}$$

which lead to effective mass parameters

$$\begin{aligned}m_{LL}^\nu &\sim \sum_i \mathcal{N}_{ei}^2 m_{\nu_i}, \quad \mathcal{N} = \mathcal{V}^{\nu\hat{\nu}} \\ m_{LL}^S &\sim -\sum_i \frac{M_{Dei}^2 M_{N_i}}{M_i^4} |p^2| \\ m_{LL}^N &\sim \sum_i \frac{M_{Dei}^2}{M_{N_i}^3} |p^2|\end{aligned}\tag{41}$$

# Non-SUSY SO(10) with extended inverse seesaw

Sterile neutrino contribution to  $0\nu\beta\beta$

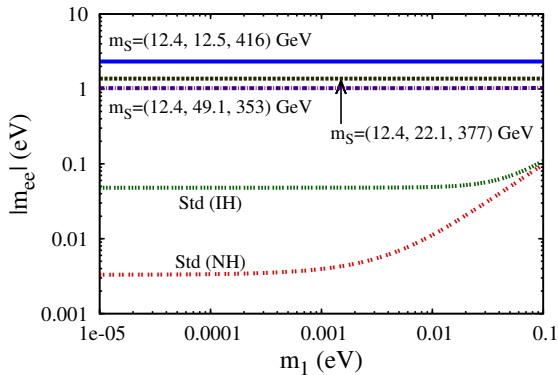


Figure : Effective mass due to sterile contribution.

# Non-SUSY SO(10) with extended inverse seesaw

Recap (Light neutrino contribution to  $0\nu\beta\beta$  and the current experimental probe)

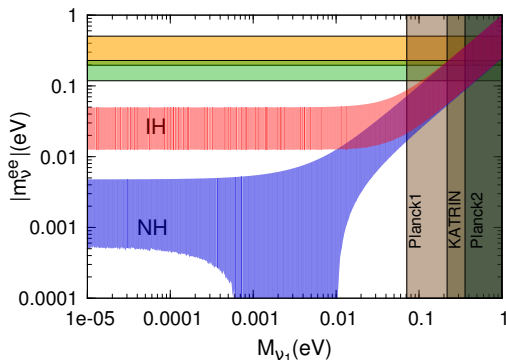


Figure : The Yellow and green horizontal bands correspond to the range of effective mass for Heidelberg Moskow result and combined  $^{136}\text{Xe}$  bound.

S. Goswami, Y. Y. Keum

# Non-SUSY SO(10) with extended inverse seesaw

Effective mass vs lightest sterile mass (Cancellation in light and sterile contributions)<sup>17</sup>

- The combined absolute effective mass

$$|m_{eff}^{ee}|^2 = |m_\nu^{ee}|^2 + |m_S^{ee}|^2 + 2|m_\nu^{ee}| \cdot |m_S^{ee}| \cos(\phi) \quad (42)$$

and may lie between  $(|m_\nu^{ee}| - |m_S^{ee}|)^2$  and  $(|m_\nu^{ee}| + |m_S^{ee}|)^2$ .



$$m_\nu^{ee} = m_1 c_{12}^2 c_{13}^2 + m_2 s_{12}^2 c_{13}^2 e^{2i\alpha_2} + m_3 s_{13}^2 e^{2i\alpha_3 + \delta_{CP}}. \quad (43)$$



$$m_S^{ee} = -|p|^2 \sum_i \nu_{ei}^{\nu \hat{s}^2} \frac{1}{M_{S_i}}. \quad (44)$$

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<sup>17</sup>Pascoli et al. (2013)

# Non-SUSY SO(10) with extended inverse seesaw

Effective mass vs lightest sterile mass (Cancellation in light and sterile contributions)

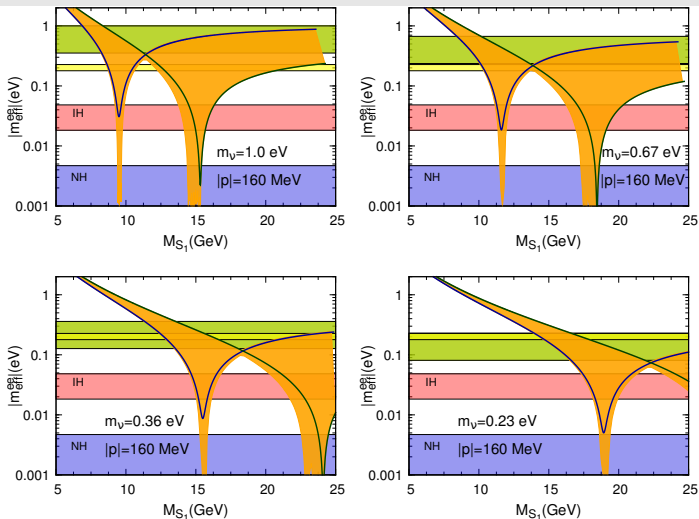


Figure : Green band → allowed light neutrino contribution. Yellow band → combined  $^{76}\text{Ge}$  experiment exclusion limit. Orange band → light+sterile contribution for fixed  $|p| = 160$  MeV. Blue curve →  $\nu$  oscillation best fit. Green curve →  $\alpha_2 = \pi/2$ ,  $\alpha_3 + \delta_{CP} = \pi/2$ .

# Non-SUSY SO(10) with extended inverse seesaw

Life-time vs lightest sterile mass

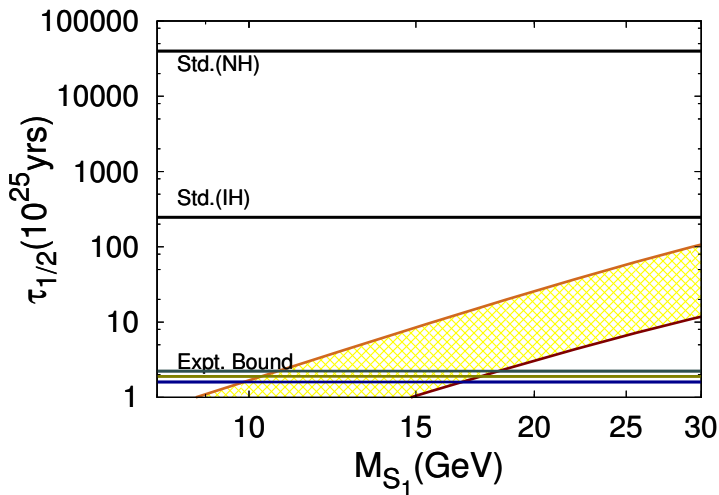


Figure : Sterile contribution in normal and inverted hierarchy scenario. Virtual momentum varies in [160 – 200] MeV range.

# Non-SUSY SO(10) with extended inverse seesaw

Life-time vs lightest sterile mass (Scatter plot)

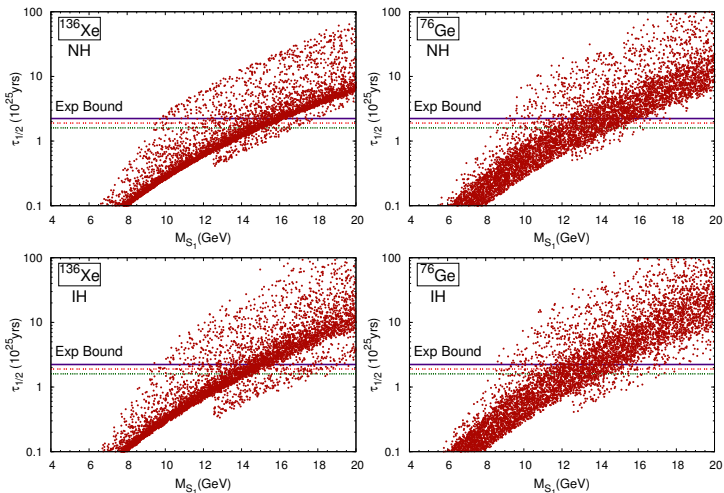


Figure : Comparative study of  $0\nu\beta\beta$  contribution due to sterile neutrino, in two popular isotopes  $^{76}\text{Ge}$  (left) and  $^{136}\text{Xe}$  (right). Normal hierarchy and inverted hierarchy solutions are assumed in going from top to bottom.

# Non-SUSY SO(10) with extended inverse seesaw

Life-time vs lightest sterile mass (Scatter plot)

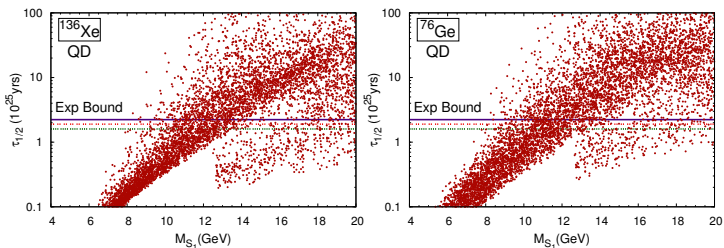


Figure : Same as previous figure but light neutrinos in quasi-degenerate ( $m_{\nu_1} = 0.23$  eV) state.

# Non-SUSY SO(10) with extended inverse seesaw

Life-time vs lightest sterile mass (Xe predictions in QD scenario)

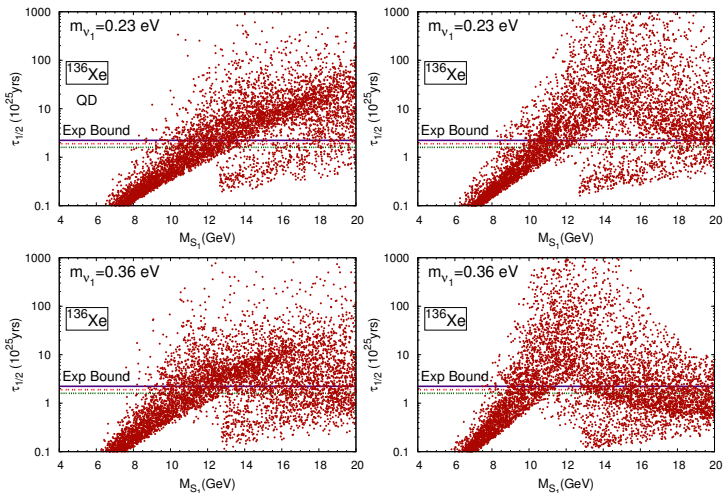


Figure : Left panel corresponds to best fit for light neutrino with zero Majorana phases. Right panel due to allowing Majorana phase  $\alpha_2, \alpha_3 \in [0, 2\pi]$ .

1. We have investigated signature of BSM physics from non-SUSY SO(10).
2. Implementation of inverse seesaw in SO(10) gives
  - $\tau_p(e^+\pi^0)$  accessible to SuperK.
  - TeV scale  $Z'$  accessible to LHC.
  - LFV decay branching ratios 3 – 6 orders smaller than the current experimental limits.
  - RH N's are Pseudo-Dirac.
3. Extended seesaw in SO(10)
  - $W_R^\pm, Z_R \sim (1.2 - 3.5) \text{ TeV}$ , accessible to LHC.
  - LFV decays branching ratios 3 – 6 order smaller than experimental limit.
  - New dominant contribution to  $0\nu\beta\beta$  due to Sterile  $\nu$ -exchange in the  $W_L - W_L$  channel.

## 3. Extended seesaw in SO(10)

- $W_R^\pm, Z_R \sim (1.2 - 3.5) \text{ TeV}$ , accessible to LHC
- LFV decays branching ratios 3 – 6 order smaller than experimental limit
- New dominant contribution to  $0\nu\beta\beta$  due to Sterile  $\nu$ -exchange in the  $W_L - W_L$  channel
- Bound  $M_{S_1} > 14 \pm 4 \text{ GeV}$
- Observable  $n - \bar{n}$  oscillation  $\tau_{n-\bar{n}} \simeq 10^8 - 10^{10} \text{ secs}$
- Current bound on rare Kaon decay branching ratio predicts PS breaking scale at  $\gtrsim 10^6 \text{ GeV}$ .
- Proton is stable and  $p \rightarrow e^+ \pi^0$  not observable in possible future if  $M_{W_R} \simeq 3 - 5 \text{ TeV}$
- But if  $M_{W_R} \geq 100 \text{ TeV}$ ,  $\tau_p \simeq 5.5 \times 10^{35 \pm 0.32} \text{ yrs}$   
(Within experimentally accessible range of SuperK and HyperK).
- All other predictions are unchanged.

A word cloud featuring the phrase "Thank You" in numerous languages. The central and largest text is "thank you" in red. Surrounding it are other languages including: "danke" (blue), "gracias" (green), "merci" (orange), "dank je" (green), "teşekkür ederim" (purple), "спасибо" (blue), "obrigado" (green), "sukriya" (purple), "go raibh maith agat" (purple), "arigatō" (purple), "dank u" (green), "mochchakkeram" (blue), "mamiun" (blue), "trugarez" (blue), "merci" (orange), "dieu" (blue), "mamiun" (blue), "mochchakkeram" (blue), "arigatō" (purple), "dank u" (green), "mochchakkeram" (blue), "arigatō" (purple), "dank u" (green), "mochchakkeram" (blue), "arigatō" (purple).